

Q2 (a) For the circuit shown in Fig.2, determine (i) its graph (ii) its oriented graph (iii) trees.

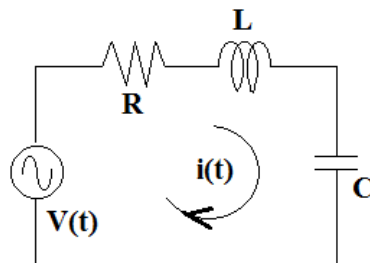
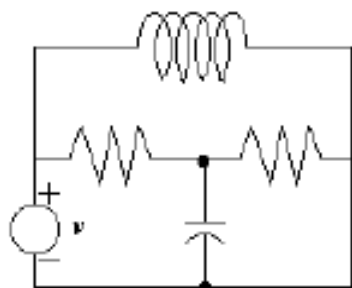


Fig.3

Answer

Q: 2 (a)

Fig. 2

(i) Graph

(ii) Oriented graph

(iii) Trees

**Q2 (b) Define duality. Obtain dual of network shown in Fig.3. Write integro-differential equation for both.**

**Answer**

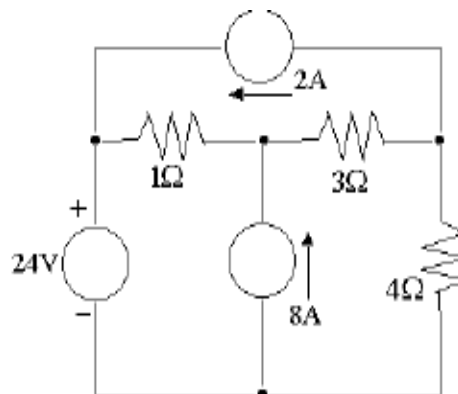
(b) Duality :- The process of converting a network from loop basis to node basis for the purpose of analysis.

Fig. 3

$$L \frac{di}{dt} + Ri + \frac{1}{C} \int i dt = v(t)$$

$$C' \frac{dv'}{dt} + G'v' + \frac{1}{L'} \int v' dt = i'(t)$$

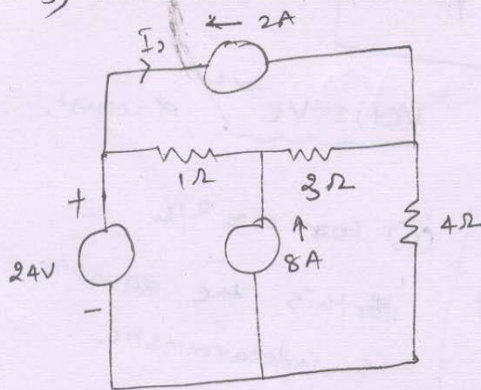
**Q2 (c) Write various steps involved for loop analysis. Find the power dissipated in the 4Ω resistor in the circuit shown in Fig.4 using loop analysis.**



## Answer

3 ⊛ Loop analysis steps:-

- 1) Select the various loops.
- 2) Show the various loop currents & the polarities of the associated voltage drops.
- 3) Search for any current source, before applying KVL to the loops.
- 4) Apply KVL to the loops that do not consist current source. Follow sign convention.
- 5) Solve the eq<sup>s</sup> obtained in steps 3 ~~and~~ <sup>and</sup> 4 simultaneously, to obtain the required unknowns.



Writing KVL to super mesh

$$-24 + 4I_3 + 3(I_3 - I_2) + 1(I_1 - I_2) = 0.$$

$$I_1 - 4I_2 + 7I_3 = 24. \quad \text{---(1)}$$

For Branches having sources

$$I_2 = -2 \quad I_3 - I_1 = 8 \quad \text{---(2)}$$

$$\text{From eq. (1)} \quad I_1 + 8I_2 + 7I_3 = 8 \quad \text{---(3)}$$

$$\text{From eq (2) \& (3).} \quad I_3 = 3 \text{ Amp.}$$

$$\text{Power dissipated in } 4\Omega \text{ resistor} = I_3^2 R = 9 \times 4 = 36 \text{ Watts.} \quad \text{Ans.}$$



Q3 (a) After steady-state current is established in the R-L circuit shown in Fig.5 with Switch S in position 'a' the switch is moved to position 'b' at  $t = 0$ . Find  $i_L(0^+)$  and  $i(t)$  for  $t > 0$ . What will be the value of  $i(t)$  when  $t = 4$  seconds?

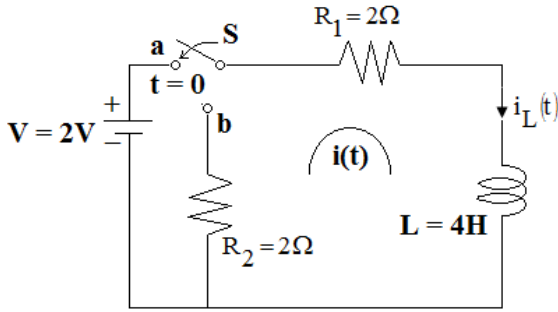


Fig.5

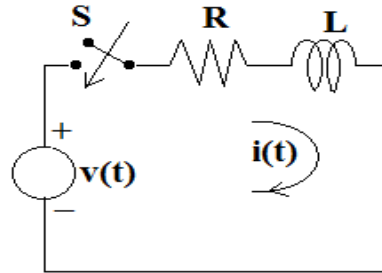


Fig.6

Answer

Q:3  
(a)

Fig.5

Writing KVL eq, when switch S is open

$$L \frac{di}{dt} + R_1 i + R_2 i = 0$$

4  $\frac{di}{dt} + 2i + 2i = 0$  (on substituting values)

$$\frac{di}{dt} + i = 0 \quad \text{--- (1)}$$

By applying Laplace Transform eq (1)

$$sI(s) - i(0^+) + I(s) = 0$$

$$\therefore I(s)(s+1) = i(0^+)$$

So the current just before switching

$$i(0) = \frac{V}{R} = \frac{2}{2} = 1 \text{ Amp.}$$

After switching to position 'b', current  $i(0^+) = 1 \text{ Amp}$  due to L. in the ckt.

$$\therefore I(s)(s+1) = 1 \Rightarrow I(s) = \frac{1}{s+1}$$

By taking Inverse LT  $i(t) = e^{-t}$

After  $t = 4$  sec,

$$i(t) = e^{-4} = \underline{\quad \quad \quad} \text{ Amp.}$$

Q3 (b) In the given network of Fig.6, the switch S is closed at t=0. The voltage source follows the law  $v(t) = Ve^{-\alpha t}$ , where  $\alpha$  is a constant. Solve for the current assuming that (i)  $\alpha \neq R/L$  (ii)  $\alpha = R/L$ .

Answer

Q:3  
(b)

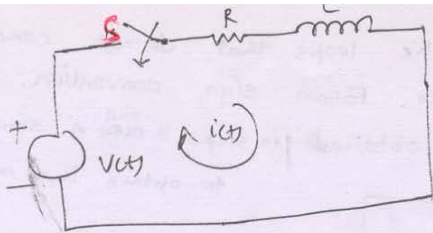


Fig. 6

Switch S is closed at t=0.  $v(t) = Ve^{-\alpha t}$ ,  $\alpha = \text{const.}$

(i)  $\alpha \neq R/L$

$v(t) = L \frac{di}{dt} + Ri$  (By writing KVL)

$\therefore Ve^{-\alpha t} = L \frac{di}{dt} + Ri$

$\therefore \frac{di}{dt} + \frac{R}{L} i = \frac{V}{L} e^{-\alpha t}$

By integrating factor  $e^{+R/Lt}$

$e^{R/Lt} \frac{di}{dt} + \frac{R}{L} i \cdot e^{R/Lt} = \frac{V}{L} e^{(\frac{R}{L} - \alpha)t}$

$i e^{R/Lt} = \frac{Ve^{(R/L - \alpha)t}}{(R/L - \alpha)} + K$

$i = \frac{Ve^{-\alpha t}}{R - \alpha L} + \frac{Ke^{-R/Lt}}{1}$

$i(0) = 0 = \frac{V}{R - \alpha L} + K$

hence  $i = \frac{V}{(R - \alpha L)} (e^{-\alpha t} - e^{-R/Lt})$

(ii) For  $\alpha = R/L$

This is the equation is indeterminate.

Using L'Hospital's rule

$i e^{+R/Lt} = \frac{Vt}{L} + K$

$i = \frac{Vt e^{-R/Lt}}{L} + K e^{-R/Lt}$

$i(0) = 0 = K$

hence

$i = \frac{Vt e^{-R/Lt}}{L}$

Q4 (a) At  $t = 0$ , a switch is closed, connecting a voltage source  $V$  to a series RC circuit. Find the expression for current by using method of Laplace transform. Assume capacitor has no initial charge.

Answer

Q: 4 (a) The given n/w will be

By writing the voltage exp.

$$\frac{1}{C} \int_{-\infty}^t i dt + Ri = Vu(t).$$

By Taking Laplace Transform

$$\frac{1}{C} \left[ \frac{I(s)}{s} + \frac{q(0^-)}{s} \right] + RI(s) = \frac{V}{s}$$

Now  $q(0^-)$  is the charge on capacitor at  $t=0^-$ .  
If the capacitor is initially uncharged  $q(0^-) = 0$ .

$$I(s) \left( \frac{1}{Cs} + R \right) = \frac{V}{s}$$

By rearranging

$$I(s) = \frac{V/R}{(s + 1/RC)}$$

Taking Inverse Laplace

$$\mathcal{L}^{-1}\{I(s)\} = \mathcal{L}^{-1}\left\{ \frac{V/R}{(s + 1/RC)} \right\}$$

$$\therefore i(t) = \frac{V}{R} e^{-t/RC} \quad t \geq 0$$

$$i(t) = 0 \quad t < 0$$

Ans.



**Q4 (b) State and prove initial value theorem and final value theorem for Laplace transform. Obtain initial value for the function  $F(s) = 2(s+1) / s^2+2s+5$**

**Answer**

(b) For initial & final value Th of Laplace Transform  
 Topic: 8.4 Reft(I)

$F(s) = \frac{2(s+1)}{s^2+2s+5}$  } Find the initial value.

$f(0^+) = \lim_{t \rightarrow 0^+} f(t) = \lim_{s \rightarrow \infty} s \cdot F(s) = \lim_{s \rightarrow \infty} \frac{2(s+1)s}{s^2+2s+5} = 2$

or By writing  $F(s) = \frac{2(s+1)}{(s+1)^2+2} \Rightarrow f(t) = 2e^{-t} \cos 2t$  hence for  $f(0^+) = \frac{2e^0 \cos 0}{1 \cdot 1} = 2$  Ans.

**Q5 (a) State and prove reciprocity theorem. Write its application.**

**Answer**

Reciprocity Theorem, Topic 9.4 of Text Book I

**Q5 (b) Obtain the transform impedance representation for a capacitor and an inductor. For initial conditions in the network, how they are transformed?**

**Answer**

Transformation of Capacitor & Inductor, Topic 9.2 of Text Book I

**Q6 (a) Discuss the time domain behaviour from the pole and zero plot.**

**Answer**

Topic 10.7 of Text book I

**Q6 (b) Determine whether the polynomial are Hurwitz or not.**

(i)  $F(s) = s^3 + 2s^2 + s + 2$

(ii)  $F(s) = s^4 + s^3 + 2s^2 + 2s + 1 = 0$

Answer

(b) Hurwitz or not ?

(i)  $F(s) = s^3 + 2s^2 + s + 2$

Using ~~con~~  $m(s) = 2s^2 + 2$  - even Part  
 $n(s) = s^3 + s$  - odd

continued Fraction Expansion =  $\frac{n(s)}{m(s)}$

$$2s^2 + 2 \overline{) s^3 + s} \left( \frac{1}{2}s \right)$$

$$\underline{s^3 + s}$$

$$0$$

By taking ratio of

$$\frac{n(s)}{m(s)} = \frac{s^3 + s}{2s^2 + 2} = \frac{s(s^2 + 1)}{2(s^2 + 1)}$$

Hence  $F(s) = \underbrace{(2s^2 + 2)}_{\text{Hurwitz}} \left( \frac{1}{2}s + 1 \right)$

Hence F(s) Hurwitz an.

(ii)  $F(s) = s^4 + s^3 + 2s^2 + 2s + 1 = 0$

Using Routh's array

$s^4$	1	2	1	
$s^3$	1	2	0	} one sign change
$s^2$	$\frac{2s-1}{s}$	1	0	
$s^1$	$\frac{2s-1}{s}$	0		} one sign change.
0	1			

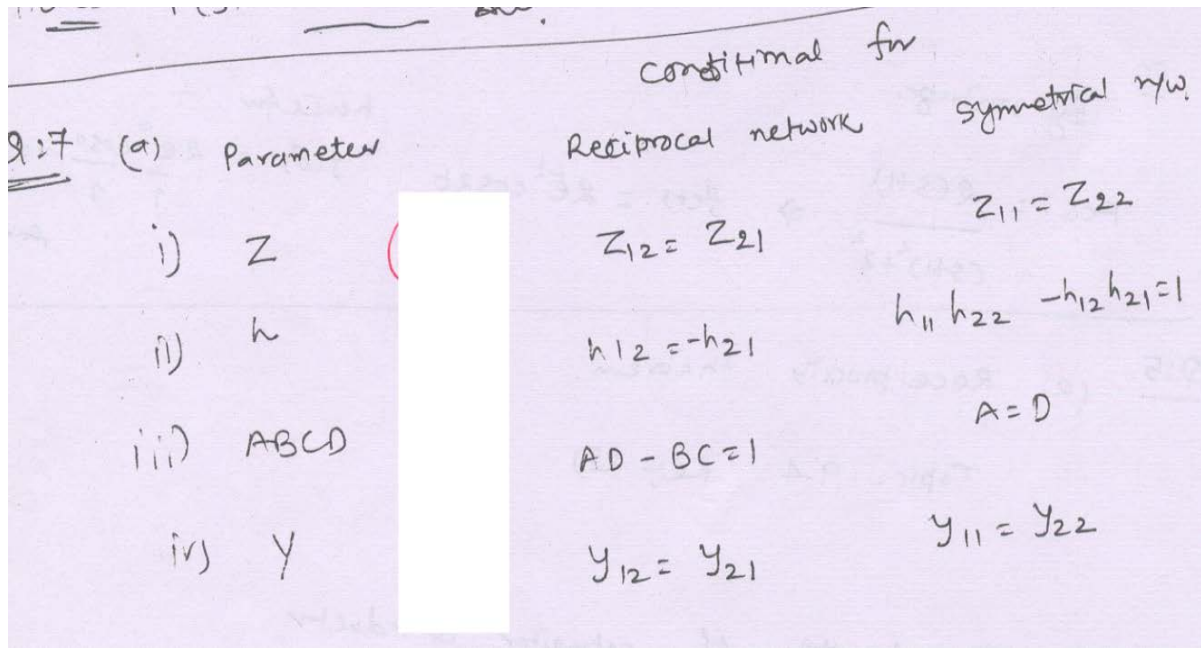
Two changes in sign implying that  $F(s)$  has two roots with positive real parts.

Hence  $F(s)$  is not a Hurwitz polynomial.



**Q7 (a) State the condition of two port network to be reciprocal and symmetrical interms of Z, h , ABCD & Y parameters.**

**Answer**

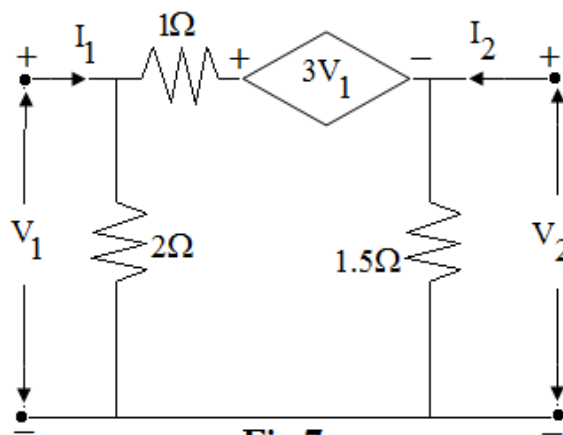


**Q7 (b) Explain twin -T network.**

**Answer**

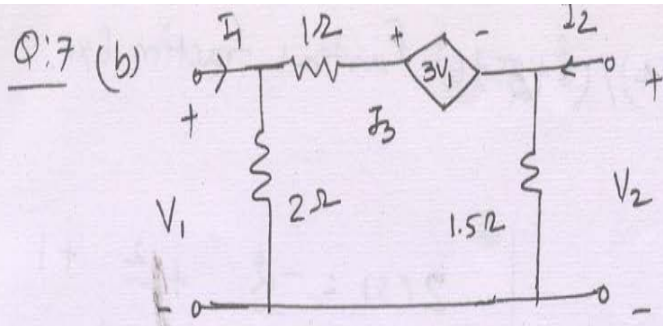
Twin T-n/w, Topic 11.7 of Text Book I

**Q7 (c) For the circuit as shown in Fig.7, find the Y-parameters.**



**Fig.7**

Answer



Y-Parameter 7/11

Let  $I_3$  be the current in middle loop.

by ~~KVL~~ applying KVL,

$$V_1 = 2(I_1 - I_3)$$

$$2(I_3 - I_1) + 1.5I_3 + 3V_1 + 1.5(I_3 + I_2) = 0$$

$$\therefore 4.5I_3 = 2I_1 - 1.5I_2 - 3V_1$$

and

$$V_2 = 1.5(I_2 + I_3)$$

using above eq.s.

$$V_1 = 0.476I_1 - 0.285I_2$$

$$V_2 = 0.19I_1 + 1.285I_2$$

$$Z = \begin{bmatrix} 0.476 & -0.285 \\ 0.19 & 1.285 \end{bmatrix}$$

$$Y = [Z]^{-1} = \begin{bmatrix} 0.476 & 0.285 \\ 0.19 & 1.285 \end{bmatrix}^{-1}$$

$$Y = \begin{bmatrix} -1.285 & -0.285 \\ 0.19 & -0.476 \end{bmatrix}$$

Bv.

Q8 (a) Obtain (i) Foster –I form realization and (ii) Cauer –II form realization for

$$Z(s) = 2(s+1)(s+3) / s(s+2)$$

Answer

Q:8 (a)  $F(s) = \frac{2(s+1)(s+3)}{s(s+2)}$   
 Poles: 0, -2 & zeros -1, -3.

Foster-I form.

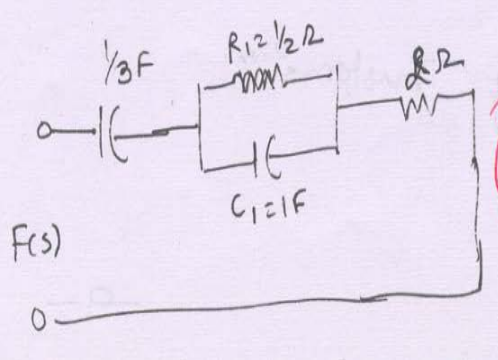
$$F(s) = \frac{2s^2 + 8s + 6}{s^2 + 2s} = 2 + \frac{4s + 6}{s(s+2)}$$

$$= Z(\infty) + F_1(s)$$

$$F_1(s) = \frac{4s + 6}{s(s+2)} = \frac{A}{s} + \frac{B}{s+2}$$

On solving  $A = 3$   $B = 1$

hence  $F(s) = 2 + \frac{3}{s} + \frac{1}{s+2}$



Cauer-II form.

$$F(s) = \frac{6 + 8s + 2s^2}{2s^2 + s^2}$$

using continued fraction expansion

$$2s^2 \overline{) 6 + 8s + 2s^2} \quad \left| \frac{3}{s} \right.$$

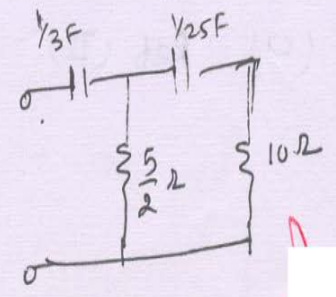
$$\underline{6 + 3s}$$

$$5s + 2s^2 \quad \left| \frac{2}{s} \right.$$

$$\underline{5s + 4}$$

$$-2s^2 \quad \left| \frac{25}{s} \right.$$

$$\underline{-\frac{1}{5}s^2} \quad \left\{ \frac{1}{10} \right.$$



Q8 (b) Synthesize  $Z(s) = (s^2 + 5s + 4) / (s^2 + 5s + 6)$  using partial fraction expansion method.



Answer

(b)  $Z(s) = \frac{(s^2 + 5s + 4)}{(s^2 + 5s + 6)}$  Partial fraction Exp.

$$Z(s) = \frac{(s+1)(s+4)}{(s+2)(s+3)}$$

$$= \frac{k_0}{s} + \frac{k_1}{s+2} + \frac{k_2}{s+3} + k_{\infty}$$

$k_0 = s \cdot Z(s) \Big|_{s \rightarrow 0} = 0$

$k_1 = (s+2) Z(s) \Big|_{s \rightarrow -2}$

$$= \frac{(s+1)(s+3)}{(s+3)} \Big|_{s \rightarrow -2} = 1$$

$k_2 = (s+3) Z(s) \Big|_{s \rightarrow -3}$

$$= 2$$

$k_{\infty} = Z(s) \Big|_{s \rightarrow \infty} = 1$

$$Z(s) = \frac{-2}{(s+2)} + \frac{2}{(s+3)} + 1$$

$$-Z(s) = \frac{2}{(s+2)} - \frac{2}{(s+3)}$$

$$Z(s) = \frac{1}{1 + \frac{2}{s}} + \frac{1}{\frac{1}{2}s + \frac{3}{2}}$$

$$= \frac{1}{1 + \frac{1}{\frac{7}{2}s}} + \frac{1}{\frac{1}{2}s + \frac{3}{2}}$$

The circuit diagram shows an input terminal with current  $i$  and voltage  $Z(s)$ . The circuit consists of two parallel branches in series. The first parallel branch contains a  $1 \Omega$  resistor and a  $\frac{1}{2} H$  inductor. The second parallel branch contains a  $\frac{3}{2} \Omega$  resistor and a  $\frac{1}{2} F$  capacitor.

**Q9 (a) Discuss how the element change in Frequency Transformations used for filter design.**

**Answer**

Frequency Transformation of Text Book II

**Q9 (b) Realise  $H(s) = s / \{s^3 + s^2 + 3s + 1\}$  as a network terminated by  $1\Omega$  resistor.**

**Answer**

Q:9 (b)

$$H(s) = \frac{s}{(s^3 + s^2 + 3s + 1)}$$

n/w terminated by  $1\Omega$  resistor

Using continued fraction

$$1 + \frac{2}{s} \left| \begin{array}{l} 3s + s^3 \\ 3s + 3s^3 \end{array} \right| \frac{3s}{2s^3}$$

$Z_{22}(s) = \frac{1}{Y_{22}(s)} = \frac{s^2 + 1}{3s + s^3}$

using case - II form

$$3s + s^3 \left| \begin{array}{l} 1 + s^2 \\ 1 + \frac{1}{3}s^2 \end{array} \right. \left( \frac{1}{3}s = \frac{1}{C_1 s} \right)$$

using case - I form

$$\frac{2}{3}s^2 \left( s^3 + 3s \right) \left( \frac{3}{2}s \leftarrow C_2 s \right)$$

$$3s \left) \frac{s^3}{\frac{2}{3}s^2} \left( \frac{2}{9}s \leftarrow L_3 s \right) \right.$$

$$\frac{-\frac{2}{3}s^2}{0}$$

ZOT at  $s=0$  &  $s=\infty$  for  $H(s)$ .  
 $n=1$   $m=3$   
 ZOT at  $s=0$  are  $n=1$   
 ZOT at  $s=\infty$  are  $m-n=2$ .

**Text Books**

- 1. Network Analysis, M.E. Van Valkenberg, 3<sup>rd</sup> Edition, Prentice-Hall India, EEE 2006.**
- 2. Network Analysis and Synthesis, Franklin F Kuo, 2<sup>nd</sup> Edition, Wiley India Student Edition 2006.**