**Q.2** a. Define Quantization. Derive the signal-to-quantization noise ratio for sinusoidal signals.

Answer: Topic 4.8.3, Page Number 219 of Text Book 1

b. In the system shown in Fig.1,  $X_{c}\left(j\Omega\right)$  and  $H(e^{j\omega})$  are as shown

and  $1/T_1 = 30000$ ,  $1/T_2 = 10000$  respectively. Sketch and label the Fourier transforms of  $y_d[n]$  and  $y_c(t)$ .

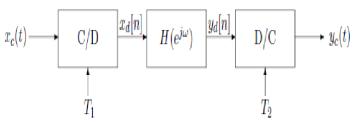


Fig.1

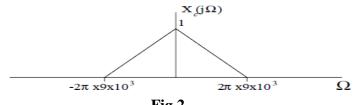


Fig.2

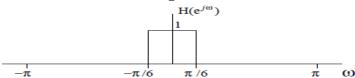
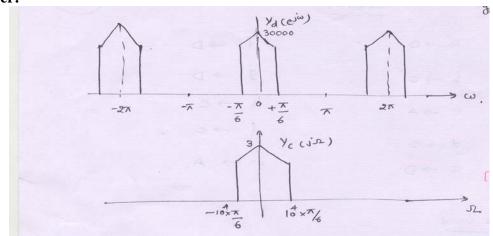


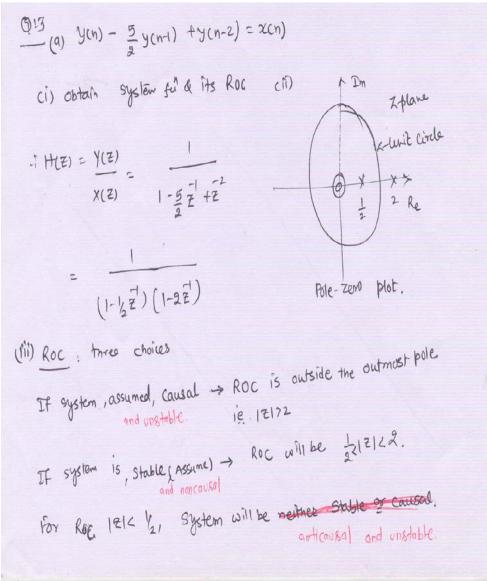
Fig.3

**Answer:** 



- Q.3 a. Consider the LTI system with input x[n] and output y[n], which are related through the difference equation: y[n] 5/2 y[n-1] + y[n-2] = x[n]
  - (i) Obtain the system function and its ROC
  - (ii) Draw its pole-zero plot
  - (iii) Comment on the causality and stability of this system

## **Answer:**



b. A discrete-time causal LTI system has the system function

$$H(z) = \frac{(1+0.2z^{-1})(1-9z^{-2})}{(1+0.81z^{-2})}$$

Find expression for a minimum-phase system  $H_1(z)$  and an all- pass system  $H_{ap}(z)$  such that  $H(z) = H_1(z) H_{ap}(z)$ .

## **Answer:**

$$H(z) = \frac{(1+0.2z^{-1})(1-3z^{-2})}{(1+0.8|z|^{-2})}$$

$$= \left[\frac{(1+0.2z^{-1})(1-3z^{-1})(1+3z^{-1})}{(1+0.8|z|^{-2})}\right] \left[\frac{(1-\frac{1}{3}z^{-1})(1+\frac{1}{3}z^{-1})}{(1-\frac{1}{3}z^{-1})(1+\frac{1}{3}z^{-1})}\right]$$

$$= \left[\frac{(1+0.2z^{-1})(1-\frac{1}{3}z^{-1})(1+\frac{1}{3}z^{-1})}{(1+0.8|z|^{-2})}\right] \left[\frac{(1-3z^{-1})(1+3z^{-1})}{(1-\frac{1}{3}z^{-1})(1+\frac{1}{3}z^{-1})}\right]$$

$$H(z) = \left[\frac{(1+0.2z^{-1})(1-\frac{1}{3}z^{-2})}{(1+0.8|z|^{-2})}\right] \left[\frac{1-9z^{-2}}{1-\frac{1}{9}z^{-2}}\right]$$

$$H(z) = H_{1}(z) H_{0p}(z)$$

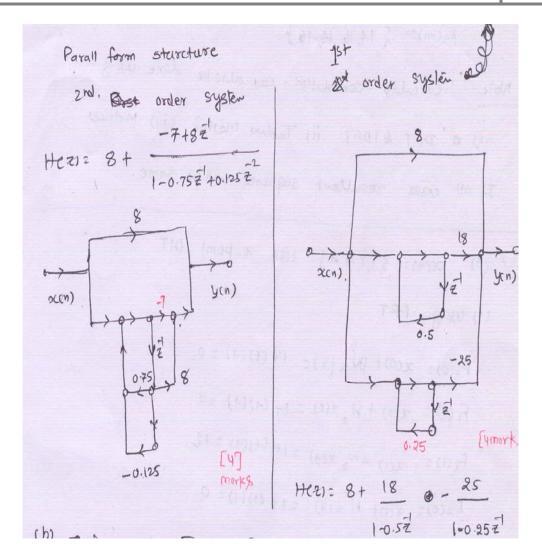
$$Uhaye H_{1}(z) = \frac{(1+0.2z^{-1})(1-\frac{1}{3}z^{-2})}{(1+0.8|z|^{-2})} \cdots minimum-phase system$$

$$H_{2}(z) = \frac{1-9z^{-2}}{1-\frac{1}{9}z^{-2}} \cdots all-pass system.$$
[68 mm]

**Q.4** a. Obtain the parallel-form structure of the given H(z) for first-order and second order systems.

$$H(z) = \frac{\left(1 + 2z^{-1} + z^{-2}\right)}{\left(1 - 0.75z^{-1} + 0.125z^{-2}\right)}$$

Answer:



b. Describe the signal flow graph representation of linear constant coefficient difference equations.

**Answer:** Topic 6.2 of Text Book 1

**Q.5** a. With an example, design a differentiator using Kaiser Window concept. **Answer:** Topic 7.3.2 of Text Book 1

b. Discuss the Parks- McClellan algorithm for type I low pass filter. **Answer:** Topic 7.4.3 of Text Book 1

Q.6 a. Discuss and prove the following properties of Discrete Fourier Transform.(i) Duality (ii) Symmetry

**Answer:** Topic 8.6.3 and 8.6.4 of Text Book 1

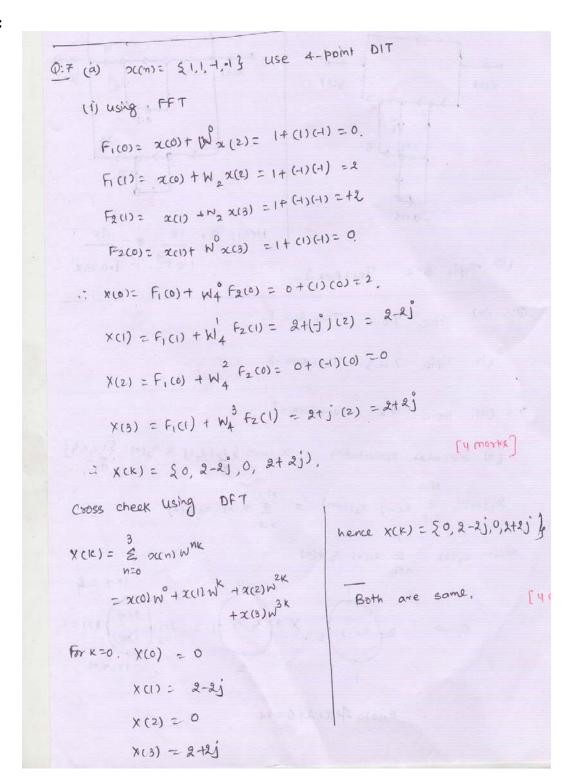
b. Perform the Circular Convolution of the two sequences  $x_1(n) = \{\underline{2}, 1, 2, 1\}$  and  $x_2(n) = \{\underline{1}, 2, 3, 4\}$ .

Answer:

(b) circular convolution 
$$x_{1}(n) = \{\frac{1}{2}, \frac{1}{2}, 1\}$$
 &  $x_{2}(n) = \{\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}\}$ 
 $X_{3}(m) = \sum_{n=0}^{3} x_{1}(n) \cdot x_{2}(m-n) = \sum_{n=0}^{3} x_{1}(n) \cdot x_{2}(n)$ 
 $x_{3}(n) = \sum_{n=0}^{3} x_{1}(n) \cdot x_{2}(n)$ 
 $x_{3}(n)$ 

**Q.7** a. For x(n) = (1,1,-1,-1) use 4-point DIT, algorithm for FFT and cross check the result using DFT.

**Answer:** 



- a. Discuss the effect of windowing on Fourier analysis of sinusoidal signals. 0.8 **Answer:** Section 10.2, Page Number 723 of Text Book 1
  - b. Discuss the time-dependent Fourier transform with a suitable example.

**Answer:** Topic 10.3 of Text Book 1

- **Q.9** b. For a real, causal sequence x(n) for which  $X_R(e^{jw}) = \frac{5}{4} \cos \omega$ . Obtain
  - (i) The original sequence x(n) and
  - (ii) Imaginary part of the Fourier transform  $X_I$  (e  $^{jw}$ ).

## **Answer:**

$$\frac{Q.9(b)}{\omega e |_{QOW}} (i) \quad \chi_{R}(e^{i\omega}) = \frac{5}{4} - \cos \omega = \frac{5}{4} - \frac{1}{2}e^{i\omega} - \frac{1}{2}e^{-i\omega}$$

$$\omega e |_{QOW}} + \cot \omega +$$

## **TEXT BOOKS**

Discrete-Time Signal Processing (1999), Oppenheim, A. V., and Schafer, R. W., with J. II R.Buck, Second Edition, Pearson Education, Low Price Edition.