Q.2 a. Show that the function  $f(z) = \sqrt{|xy|}$  is not analytic at the origin even though Cauchy-Riemann equations are satisfied thereof.

### Answer: Page Number 742 of Text Book I

**Q.3** a. Find Laurent's series expansion of  $\frac{z^2-1}{z^2+5z+6}$  about z=0 in the

region 2 < |z| < 3.

Answer: Page Number 778 of Text Book I

b. Use Residue theorem to evaluate 
$$\int_{C} \frac{1-2z}{z(z-1)(z-2)} dz, C: |z| = 1.5$$

### Answer: Page Number 784 of Text Book I

**Q.4** a. If  $u = x^2 + y^2 + z^2$  and V = xI + yJ + zK, show that div(uV) = 5uAnswer: Page Number 363 of Text Book I

b. Find the angle between the normals to the surface  $xy = z^2$  at the points (4, 1, 2) and (3,3,-3).

#### Answer: Page Number 354 of Text Book I

**Q.5** a. Apply Green's theorem to evaluate 
$$\int_{C} \left[ (3x - 8y^2) dx + (4y - 6xy) dy \right]$$

Where C is the boundary of the region bounded by x=0, y=0, x+y=1Answer: Page Number 371 of Text Book I

**Q.6** a. Use Newton's divided difference formula to evaluate f(8) given that

Х	4	5	7	10	11	13		
f(x)	48	100	294	900	1210	2028		

## Answer: Page Number 1068 of Text Book I

b. Find an approximate value of log<sub>e</sub> 5 by calculating to four decimal places,

by Simpson's  $\frac{1}{3}$ rd rule,  $\int_{0}^{5} \frac{dx}{4x+5}$  dividing the range into ten equal parts.

# Answer: Page Number 1302 of Text Book II

**Q.7** a. Apply Charpit's method to solve  $(a^2 + b^2)y = bz$ . Answer: Page Number 644 of Text Book I b. Use method of separation of variables to solve  $\frac{\partial u}{\partial x} = 4 \frac{\partial u}{\partial y}$ , given that

$$\mathsf{u}(0,\mathsf{y}) = 8\mathrm{e}^{-3\mathrm{y}}.$$

## Answer: Page Number 658 of Text Book I

- **Q.8** a. A committee consists of 9 students two of which are from 1<sup>st</sup> year, three from 2<sup>nd</sup> year and four from 3<sup>rd</sup> year. Three students are to be removed at random. What is the chance that
  - (i) the three students belong to different classes.
  - (ii) two belong to the same class and third to the different class.

### Answer: Page Number 940-941 of Text Book I

b. In a certain college, 4% of the boys and 1% of girls are taller than 1.8m. Moreover 60% of the students are girls. If a student is selected at random and is found to be taller than 1.8m, what is the probability that the student is a girl?

#### Answer: Page Number 952 of Text Book I

**Q.9** a. Fit a Poisson distribution to the set of observations:

Х	0	1	2	3	4
f	122	60	15	2	1

## Answer: Page Number 966 of Text Book I

b. Assuming that the diameters of 1000 brass plugs taken consecutively from a machine, form a normal distribution with mean 0.7515 cm and standard deviation 0.0020 cm, how many of the plugs are likely to be rejected if the approved diameter is  $0.752 \pm 0.004$  cm? (Given: if z is the normal variable, then area under normal curve for  $0 \le z \le 1.75$  is 0.4599 and for  $0 \le z \le 2.25$  is 0.4878.)

Answer: Page Number 975 of Text Book I

# <u>Text Book</u>

1. Higher Engineering Mathematics –Dr. B.S.Grewal, 40th Edition 2007, Khanna Publishers, Delhi.

2. A Text book of engineering Mathematics – N.P. Bali and Manish Goyal , 7th Edition 2007, Laxmi Publication(P) Ltd.