

**AMIETE – ET (OLD SCHEME)**

Time: 3 Hours

**OCTOBER 2012**

Max. Marks: 100

**PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.**

**NOTE: There are 9 Questions in all.**

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

**Q.1 Choose the correct or the best alternative in the following: (2×10)**

a. Consider the following statements:

- (i) A switch expression can be of any type.
- (ii) The default case is optional in the switch statement.

Which of the following statements are correct?

- (A) (i) only
- (B) (ii) only
- (C) Both (i) & (ii)
- (D) None of these

b. The error quantity which must be added to the finite representation of a computed number in order to make it the true representation of that number is called.

- (A) relative error
- (B) absolute error
- (C) round-off error
- (D) truncation error

c. Consider the following statements.

- (i) C is a free-form language
- (ii) In a C program, # define is a preprocessor compiler directive

Which of the following statements are correct?

- (A) (i) only
- (B) (ii) only
- (C) (i) and (ii) both
- (D) none the these

d. In bisection method, if the permissible error is  $\epsilon$ , then the approximate number of iteration may be determined from the formula. [It is assumed that a root of  $f(x)=0$  lies in the interval  $(a_0, b_0)$  and  $n$  denotes the number of iterations]

- (A)  $n \geq \frac{\log(b_0 - a_0) - \log \epsilon}{\log 2}$
- (B)  $n \leq \frac{\log(b_0 - a_0) - \log \epsilon}{\log 2}$
- (C)  $n \geq \frac{\log(b_0 + a_0) - \log \epsilon}{\log 2}$
- (D)  $n \leq \frac{\log(b_0 + a_0) - \log \epsilon}{\log 2}$

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- e. Consider the following statements:  
 (i) If a matrix A is diagonally dominant then no pivoting is necessary  
 (ii) If a matrix A is real, symmetric and positive definite then no pivoting is necessary  
 Which of the above statements are correct?
- (A) (i) only (B) (ii) only  
 (C) Both (i) & (ii) (D) None of these
- f. The Cholesky factorisation of a symmetric matrix A is  $A = LL^T$
- If  $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 8 & 22 \\ 3 & 22 & 82 \end{bmatrix}$  and  $L = \begin{bmatrix} 1 & 0 & 0 \\ 2 & a & 0 \\ 3 & b & c \end{bmatrix}$ ,  $a < 0, c > 0$ ,  
 then, the values of (a,b,c) are
- (A) (2, 8, 3) (B) (2, 4, 3)  
 (C) (2, -8, -3) (D) (2, -4, 3)
- g. Netwon's backward difference formula
- (A) can be expressed in terms of forward differences  
 (B) is more suitable when we have to interpolate at a point nearer to the initial point  
 (C) is more suitable when we have to interpolate at a point nearer to the end point  
 (D) does not give identical polynomial as obtained by using Netwon's forward difference formula
- h. Consider the following values for the function  $f(x) = x^4$ .
- | X   | f(x)   |
|-----|--------|
| 0.4 | 0.0256 |
| 0.6 | 0.1296 |
| 0.8 | 0.4096 |
- The approximate value of  $f'(0.8)$  using the method based on quadratic interpolation is
- (A) 1.84 (B) 2.048  
 (C) 1.82 (D) 4.4
- i. Find the approximate value of
- $$I = \int_0^1 \frac{dx}{1+x}$$
- Using Simpson's rule
- (A) 0.75 (B) 0.7050  
 (C) 0.6915 (D) 0.6944

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- j. Which of the method use a weighted average of slopes on the given interval, instead of a single slope?

(A) Taylor's method                      (B) Runge-Kutta method  
(C) Euler's Method                      (D) None of these

**Answer any FIVE Questions out of EIGHT Questions.**

**Each question carries 16 marks.**

- Q.2** a. Write a C program to calculate the real roots of the equation  $e^x - 3x^2 = 0$  using bisection method. Use an error tolerance of  $\epsilon = 10^{-5}$ , maximum number of iterations 40 and  $[0,1]$  as the interval containing the root. (8)

- b. Find the iterative methods based on Newton – Raphson method for finding  $N^{1/k}$ , where N is a positive real number. Hence, estimate  $N=18$  for  $K=3$ , correct to two decimal places. (8)

- Q.3** a. Give the applications of linked lists with suitable examples. (8)

- b. Determine the inverse of the matrix

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 4 & 3 & -1 \\ 3 & 5 & 3 \end{bmatrix}$$

using partition method. Hence solve the system of equation  $Ax = b$ , where  $b = [1, 6, 4]^T$  (8)

- Q.4** a. Solve the following system of equations by LU decomposition Method. (8)

$$x_1 + x_2 - 2x_3 = 3$$

$$4x_1 - 2x_2 + x_3 = 5$$

$$3x_1 - x_2 + 3x_3 = 8$$

- b. Solve the following system of equation using Gauss-Seidel method (show upto 3 iterations),

$$4x_1 + x_2 + 2x_3 = 4$$

$$x_1 + x_2 + 3x_3 = 3 \quad (8)$$

$$3x_1 + 5x_2 + x_3 = 7$$

- Q.5** a. Expand  $\ln(1+x)$  in a Taylor series expansion about  $x_0 = 1$  through terms of degree 4. Obtain a bound on the truncation error when approximating  $\ln(1.2)$  using this expansion. (8)

- b. By use of repeated Richardson extrapolation, find  $f''(0.3)$  from the following values:

x	f(x)
0.1	17.60519
0.2	17.68164
0.3	17.75128
0.4	17.81342
0.5	17.86742

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Apply the approximate formula  $f''(x) \approx \frac{f(x+h) - 2f(x) + f(x-h)}{h^2}$  (8)

**Q.6** a. Obtain the linear least square approximation to  $f(x) = e^x$ ,  $-1 \leq x \leq 1$ . (8)

b. For the following data, calculate the difference and obtain the forward difference polynomial, using the first four points. Hence interpolate at  $x=0.25$ . (8)

x	f(x)
0.1	9.9833
0.2	4.9667
0.3	3.2836
0.4	2.4339
0.5	1.9177

**Q.7** a. Calculate the  $n^{\text{th}}$  divided difference of  $f(x) = \frac{1}{x}$  (8)

b. Evaluate the integral  $I = \int_0^{\pi} e^x \cos x dx$  using Gauss – Legendre three point formula. (8)

**Q.8** a. Evaluate the integral  $I = \int_0^1 x^3 \sqrt{x} dx$  using Simpson's rule taking eight intervals. Also obtain upper bound of the error. (8)

b. Given the following values of  $f(x) = \ln x$ , find the approximate value of  $f''(2.0)$  using quadratic interpolation. Also obtain an upper bound on the error. (8)

x	f(x)
2.0	0.69315
2.2	0.78846
2.6	0.95551

**Q.9** a. Given  $\frac{dy}{dx} = \frac{1}{x+y}$  where  $y(0) = 1$ , find  $y(0.5)$  and  $y(1.0)$  using Runge – Kutta fourth order method, (take  $h = 0.5$ ). (8)

b. Given the following equation  $x^4 - x - 10 = 0$ , determine the initial approximations for finding the smallest positive root. Use these to find the root correct to three decimal places with Secant method. (8)