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## AMIETE - ET/CS/IT (OLD SCHEME)

Time: 3 Hours
JUNE 2012
Max. Marks: 100
please write your roll no. at the space provided on each PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q. 1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the $\mathbf{Q} .1$ will be collected by the invigilator after 45 Minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.
Q. 1 Choose the correct or the best alternative in the following:
a. A system $y(n)=x(-n)$ is
(A) Causal
(B) Non Causal
(C) Both
(D) None
b. Step function $\mathrm{u}(\mathrm{t})$ is obtained from impulse function $\delta(\mathrm{t})$ by
(A) Integrating
(B) Differentiating
(C) Double Integration
(D) Differentiating twice
c. A system $y(t)=t x(t)$ is
(A) Non linear
(B) Unstable
(C) Linear
(D) Both (A) and (B)
d. A signal that violates the first Dirichlet condition i.e. $\mathrm{x}(\mathrm{t})$ must be absolutely integrable is
(A) $\mathrm{t}^{2}$
(B) t
(C) $\mathrm{t}^{3}$
(D) $1 / \mathrm{t}$
e. The frequency response of discrete time filters must be periodic with period
(A) $2 \pi$
(B) $\pi$
(C) $\pi / 2$
(D) $3 \pi / 2$
f. The FT of a periodic impulse train in time domain with period T is a periodic impulse train in frequency domain with period
(A) $4 \pi / \mathrm{T}$
(B) $\pi / \mathrm{T}$
(C) $3 \pi / \mathrm{T}$
(D) $2 \pi / \mathrm{T}$
g. The Frequency response of an LTI system with impulse response $h(t)=e^{-t} u(t)$ is
(A) $1 /(\mathrm{j} \omega+1)$
(B) $1 /(\mathrm{j} \omega-1)$
(C) $1 /(1-\mathrm{j} \omega)$
(D) $1 /\left(\mathrm{e}^{\mathrm{j} \omega}+1\right)$


## ROLL NO.

h. FT is used to convert from Time domain to frequency domain, the signals which are
(A) Periodic
(B) Aperiodic
(C) Both
(D) None
i. Step response of a first order system
(A) Always exhibits Ringing Effect
(B) Does not exhibit Ringing Effect
(C) Sometimes exhibits Ringing Effect
(D) Sometimes does not exhibit Ringing Effect
j. For a signal which is bandlimited to a frequency of 100 Hz , the Nyquist Rate will be
(A) 100 Hz
(B) 200 Hz
(C) 50 Hz
(D) 150 Hz

## Answer any FIVE Questions out of EIGHT Questions. <br> Each question carries 16 marks.

Q. 2 a. (i) Show that any real signal $\mathrm{x}(\mathrm{t})$ is composed of its even and odd parts.
(ii) Find out the energy of the signal $x(t)=e^{-3 t} u(t)$.
b. Give the five classification of systems with an example of each.
Q. 3 a. Find out the linear convolution of $x(n)=\{1,2,3,-6\}$ with $h(n)=\{2,1,-1$, $3,5\}$
b. Enlist the properties of continuous time Fourier series.
Q. 4 a. Find out the response $y(t)$ of an LTI system with impulse response $h(t)=e^{-a t} u(t) ; a>0$ to the input signal $x(t)=e^{-b t} u(t) ; b>0$
b. (i) Prove the Multiplication property of DTFT.
(ii) Find the DTFT of $x(n)=u(n-2)-u(n-6)$
Q. 5 a. Give the time domain and frequency domain analysis of First order Continuous-Time systems.
b. Explain Sampling theorem. How is sampling done with Zero Order Hold? What is Aliasing?
Q. 6 a. (i) Find out the LT of $x(t)=3 e^{-2 t} u(t)-2 e^{-t} u(t)$ and sketch the ROC in $s-$ plane.
(ii) Find out the Inverse LT of $X(s)=\frac{1}{(s+1)(s+2)}$ when ROC: $\operatorname{Re}(s)>-1$
b. Find the LT of $\mathrm{x}(\mathrm{t})=\mathrm{t} \mathrm{e}^{-\mathrm{at}} \mathrm{u}(\mathrm{t})$ using the properties of LT.
Q. 7 a. (i) If $X(z)=2+3 z^{-1}+4 z^{-2}$. Find the initial and final values of the corresponding sequence $x(n)$.
(ii) Find the z transform of $\mathrm{x}(\mathrm{n})=7(1 / 3)^{\mathrm{n}} \mathrm{u}(\mathrm{n})-6(1 / 2)^{\mathrm{n}} \mathrm{u}(\mathrm{n})$
b. Using partial fraction expansion method determine the inverse $z$ - transform

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\begin{equation*}
\text { of } X(z)=\frac{3-\frac{5}{6} z^{-1}}{\left(1-\frac{1}{4} z^{-1}\right)\left(1-\frac{1}{3} z^{-1}\right)}|z|>\frac{1}{3} \tag{8}
\end{equation*}
$$

Q. 8 a. (i) Find the Fourier transform of the signal $x(t)$
(ii) Find the convolution using waveform method of signals $x(t)=e^{-a t} u(t)$ and $\mathrm{h}(\mathrm{t})=\mathrm{tu}(\mathrm{t})$.

b. Find mean, variance and standard deviation of uniform PDF in $[-2 n, 2 n]$.
Q. 9 a. Define mean of a strictly stationary random process $\mathrm{X}(\mathrm{t})$. Also define Autocorrelation function and mention its properties.
b. What is Power Spectral Density? Give its properties.

