

Subject: ENGINEERING MATHEMATICS - II

Time: 3 Hours

Max. Marks: 100

JUNE 2011

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q.1 Choose the correct or the best alternative in the following: (2×10)

a. The value of the $\lim_{x \rightarrow 0} \frac{8^x - 2^x}{x}$ is

- (A) $\log 4$ (B) $\log 2$
(C) $\log 6$ (D) $\log 8$

b. If $y = \cos(\sin x)$, then $\frac{dy}{dx}$ is equal to

- (A) $\cos x \cdot \sin x$ (B) $-\sin(\sin x) \cdot \cos x$
(C) $\sin^2 x \cdot \cos x$ (D) $\cos^2 x \cdot \sin x$

c. If $z = 1 + i\sqrt{3}$, then $z^2 + 4$ is equal to

- (A) $z\sqrt{3}$ (B) $3z$
(C) $2z$ (D) $4z$

d. The principal argument of $-2i$ is equal to

- (A) $-\pi/3$ (B) $-\pi/2$
(C) $\pi/2$ (D) $\pi/3$

e. If $|\vec{a} + \vec{b}| = 60$, $|\vec{a} - \vec{b}| = 40$ and $|\vec{b}| = 46$, then $|\vec{a}|$ is equal to

- (A) 24 (B) 42
(C) 22 (D) 26

f. The value of $\int_0^{\pi/2} \sin^2 x dx$ is

- (A) $\pi/4$ (B) $\pi/2$
(C) $\pi/3$ (D) $\pi/6$

g. If the roots are 2, 3 then complementary function is equal to

- (A) $c_1e + c_2e^{5x}$ (B) $c_1e^x + c_2e^{5x}$
(C) $c_1e^{2x} + c_2e^{3x}$ (D) $c_1e^{x^1} + c_2e^{x^2}$

h. The period of the function of $|\cos x|$ is equal to

- (A) π (B) 2π
(C) 3π (D) 4π

i. $L\{4 \cos 5t\}$ is equal to

- (A) $\frac{5s}{s^2 + 16}$ (B) $\frac{2s}{s^2 + 16}$
(C) $\frac{4s}{s^2 + 16}$ (D) $\frac{4s}{s^2 + 25}$

j. $L^{-1}\left\{\frac{5}{s+3}\right\}$ is equal to

- (A) $3e^{-5t}$ (B) $5e^{3t}$
(C) $5e^{-3t}$ (D) $3e^{5t}$

Answer any FIVE Questions out of EIGHT Questions.
Each question carries 16 marks.

Q.2 a. Verify Rolle's theorem for $f(x) = (x-1)(x-2)(x-3)$ (8)

b. Using Maclaurin's series, expand in the power series of $\sin x$. (8)

Q.3 a. Evaluate $\int_0^{\pi} \theta \sin^4 \theta \cdot \cos^6 \theta d\theta$ (8)

b. Find the length of the curve $x = a \cos^3 \theta, y = a \sin^3 \theta$, in the first quadrant. (8)

- Q.4** a. If n is positive integer, prove that

$$(\sqrt{3} + i)^n + (\sqrt{3} - i)^n = 2^{n+1} \cos \frac{n\pi}{6}, (i = \sqrt{-1}) \quad (8)$$
- b. The impedances $z_1 = 10 - j60$ and $z_2 = 10 + j20$ are connected in parallel across a 200 volts a.c. supply. Calculate
 (i) current in each branch and the total current and
 (ii) power consumed in each branch. (8)
- Q.5** a. Show that the four points $2\vec{a} + 3\vec{b} - \vec{c}$, $\vec{a} - 2\vec{b} + 3\vec{c}$, $3\vec{a} + 4\vec{b} - 2\vec{c}$ and $\vec{a} - 6\vec{b} + 6\vec{c}$ are coplanar. (8)
- b. A force given by $3\hat{i} + 2\hat{j} - 4\hat{k}$ is applied at the point $(1, -1, 2)$. Find the moment of the force about the point $(2, -1, 3)$. (8)
- Q.6** a. Solve the differential equation $\frac{d^2y}{dx^2} + \frac{dy}{dx} + y = \cos 2x$. (8)
- b. The differential equation for a circuit in which self inductance neutralize each other is $L \frac{d^2I}{dt^2} + \frac{I}{C} = 0$. Find the current I as a function of t , given that I_m is the maximum current and $I = 0$ when $t = 0$. (8)
- Q.7** a. Find the Fourier series representing $f(x) = x$, $0 < x < 2\pi$ and sketch its graph from $x = -\pi$ to $x = 4\pi$. (8)
- b. Expand $f(x) = e^x$ in a cosine series over $(0, 1)$. (8)
- Q.8** a. Find Laplace transform of $\sin 3t \cos 5t$ (8)
- b. Find Laplace transform of $\frac{1 - e^{2t}}{t}$ (8)
- Q.9** a. Find $L^{-1} \left[\frac{s}{s^4 + s^2 + 1} \right]$ (8)
- b. Solve the differential equation using Laplace transform method,

$$\frac{d^2y}{dt^2} + 4y = \sin t, y(0) = 1, y'(0) = 0 \quad (8)$$