

Time: 3 Hours

DECEMBER 2013

Max. Marks: 100

PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q.1 Choose the correct or the best alternative in the following: (2×10)

- a. One to one mapping is obtained using
- | | |
|--------------------------------|----------------------|
| (A) Impulse invariance mapping | (B) Bilinear mapping |
| (C) Both (A) and (B) | (D) None of these |
- b. Delay distortion
- | | |
|-------------------------------------|-------------------------------------|
| (A) shift the sequence in frequency | (B) shift the sequence in phase |
| (C) shift the sequence in time | (D) shift the sequence in magnitude |
- c. The direct Form - II realization requires _____ memory than the Direct Form -I realization.
- | | |
|----------|------------------------------------|
| (A) more | (B) less |
| (C) same | (D) can not decide from given data |
- d. If the continuous time signal is $x_c(t) = \cos(16000\pi t)$ with sampling period $T = 1/6000$, will result in
- | | |
|-------------------|-------------------------------|
| (A) inequality | (B) aliasing |
| (C) interpolation | (D) recovery without aliasing |
- e. In overlap add method _____ is performed.
- | | |
|--------------------------|------------------------|
| (A) circular convolution | (B) linear convolution |
| (C) Zero padding | (D) Both (B) and (C) |
- f. Window methods are used for
- | | |
|----------------------------------|----------------------|
| (A) low pass filter | (B) high pass filter |
| (C) Linear-phase low pass filter | (D) All of these |
- g. For DIT and DIF algorithms
- | | |
|---|---------------------------------|
| (A) They involves same number of computations | (B) They requires bit reversing |
|---|---------------------------------|

- (C) They require multiplication of phase factor
 (D) All of these
- h. Time dependent Fourier Transform can be analyzed using
 (A) Overlap save method (B) Overlap add method
 (C) Both (A) & (B) (D) None of these
- i. Estimation of power density spectrum is called
 (A) auto-correlation (B) randomization
 (C) periodogram (D) spectrogram
- j. An ideal Hilbert transformer is _____ that imparts a ___ phase shift on the input signal
 (A) an all-pass filter, 90° (B) an all-pass filter, -90°
 (C) a low-pass filter, 90° (D) a low-pass filter, -90° .

**Answer any FIVE Questions out of EIGHT Questions.
 Each question carries 16 marks.**

- Q.2** a. Define Quantization. Derive the signal-to-quantization noise ratio for sinusoidal signals. (8)
- b. In the system shown in Fig.1, $X_c(j\Omega)$ and $H(e^{j\omega})$ are as shown (8)
 and $1/T_1 = 30000$, $1/T_2 = 10000$ respectively.
 Sketch and label the Fourier transforms of $y_d[n]$ and $y_c(t)$.

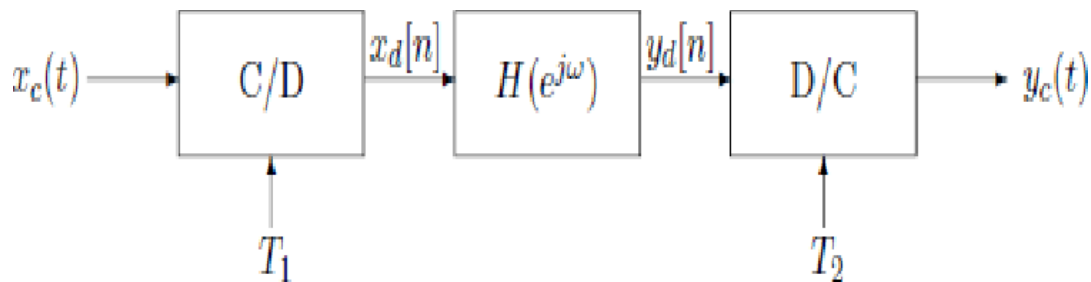


Fig.1

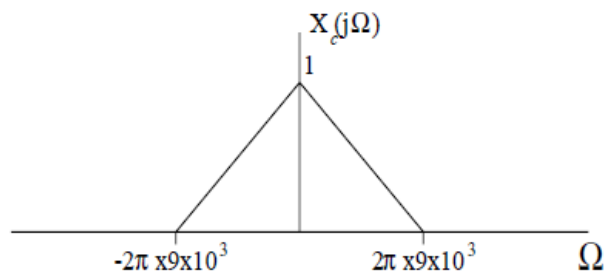


Fig.2

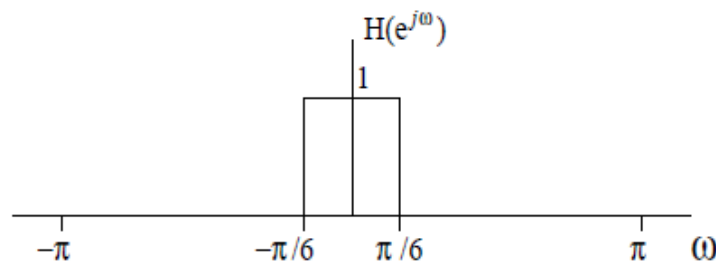


Fig.3

- Q.3** a. Consider the LTI system with input $x[n]$ and output $y[n]$, which are related through the difference equation: $y[n] - 5/2 y[n-1] + y[n-2] = x[n]$
- Obtain the system function and its ROC (4)
 - Draw its pole-zero plot (2)
 - Comment on the causality and stability of this system (2)

- b. A discrete-time causal LTI system has the system function

$$H(z) = \frac{(1 + 0.2z^{-1})(1 - 9z^{-2})}{(1 + 0.81z^{-2})}$$

Find expression for a minimum-phase system $H_1(z)$ and an all-pass system $H_{ap}(z)$ such that $H(z) = H_1(z) H_{ap}(z)$. (8)

- Q.4** a. Obtain the parallel-form structure of the given $H(z)$ for first-order and second order systems.

$$H(z) = \frac{(1 + 2z^{-1} + z^{-2})}{(1 - 0.75z^{-1} + 0.125z^{-2})} \quad (8)$$

- b. Describe the signal flow graph representation of linear constant coefficient difference equations. (8)

- Q.5** a. With an example, design a differentiator using Kaiser Window concept. (8)

- b. Discuss the Parks- McClellan algorithm for type I low pass filter. (8)

- Q.6** a. Discuss and prove the following properties of Discrete Fourier Transform. (8)
(i) Duality (ii) Symmetry

- b. Perform the Circular Convolution of the two sequences $x_1(n) = \{2, 1, 2, 1\}$ and $x_2(n) = \{1, 2, 3, 4\}$. (8)

- Q.7** a. For $x(n) = (1, 1, -1, -1)$ use 4-point DIT, algorithm for FFT and cross check the result using DFT. (8)

- b. Write a short note on implementation of DFT using “The Chirp Transform Algorithm.” (8)

- Q.8** a. Discuss the effect of windowing on Fourier analysis of sinusoidal signals. (8)

- b. Discuss the time-dependent Fourier transform with a suitable example. (8)
- Q.9** a. Explain usages of Hilbert Transform for band pass signals. (8)
- b. For a real, causal sequence $x(n)$ for which $X_R(e^{j\omega}) = \frac{5}{4} - \cos \omega$. Obtain
- (i) The original sequence $x(n)$ and
 - (ii) Imaginary part of the Fourier transform $X_I(e^{j\omega})$. (8)