

DipIETE – ET/CS (Current Scheme)

Time: 3 Hours

DECEMBER 2018

Max. Marks: 100

PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q.1 Choose the correct or the best alternative in the following: (2×10)

a. The value of $\lim_{x \rightarrow \infty} \frac{\log x}{x}$ is

- (A) 2 (B) -1
(C) 1 (D) 0

b. If $f(x) = f(2a - x)$, then $\int_0^{2a} f(x) dx$ is equal to

- (A) $\int_a^0 f(2a - x) dx$ (B) $2 \int_0^a f(x) dx$
(C) $-\int_0^a f(x) dx$ (D) 0

c. The particular Integral of the differential equation $(D^2 + 4)y = \cos 2x$

- (A) $\frac{x}{4} \cos 2x$ (B) $-\frac{x}{4} \cos 2x$
(C) $\frac{x}{4} \sin 2x$ (D) $-\frac{x}{4} \sin 2x$

d. The value of 'c' for which the Rolle's theorem is applicable for the function $f(x) = x^2 - 6x - 8$ in the interval [2, 4] is

- (A) 3 (B) 2.5
(C) 2.4 (D) None of these

e. If $\vec{A} = 4i + 3j + k$, $\vec{B} = 2i - 2j + 2k$, then the unit vector perpendicular to both \vec{A} and \vec{B} is

- (A) $8i + 6j - 14k / \sqrt{296}$ (B) $8i - 6j - 14k / \sqrt{296}$
(C) $8i + 6j + 14k / \sqrt{296}$ (D) $8i - 6j + 14k / \sqrt{296}$

- f. The value of $|A \times B|^2 + |A \bullet B|^2$ is equal to
 (A) $|A|^2|B|^2$ (B) $2|A||B|$
 (C) $4|A||B|$ (D) $4|A|^2|B|^2$
- g. The real part of $(\sin x + i \cos x)^5$ is
 (A) $-\cos 5x$ (B) $-\sin 5x$
 (C) $\sin 5x$ (D) $\cos 5x$
- h. If $f(x) = x^2$, in $-2 < x < 2$, $f(x+4) = f(x)$, then a_n is equal to
 (A) $\int_0^2 x^2 \sin \frac{n\pi x}{2} dx$ (B) $\int_0^2 x^2 \cos \frac{n\pi x}{2} dx$
 (C) $\int_0^4 x^2 \cos \frac{n\pi x}{2} dx$ (D) $\int_0^4 x^2 \sin \frac{n\pi x}{2} dx$
- i. If value of $L\{F(t)\} = f(s)$, then $L\{(\sinh at)F(t)\}$ is equal to
 (A) $\frac{1}{2}[f(s-a) - f(s+a)]$ (B) $\frac{1}{2}[f(s-a) + f(s+a)]$
 (C) $-\frac{1}{2}[f(s-a) - f(s+a)]$ (D) $\frac{1}{2}[f(s+a) - f(s-a)]$
- j. The maximum value of $L^{-1}\left\{\frac{1}{(s-a)^2 + b^2}\right\}$ is equal to
 (A) $e^{at} \sin bt$ (B) $e^{at} \cos bt$
 (C) $\frac{1}{b}e^{at} \sin bt$ (D) $\frac{1}{b}e^{at} \cos bt$

**Answer any FIVE questions out of EIGHT Questions.
 Each Question carries 16 marks.**

- Q.2** a. Use Maclaurin's series, expand $\tan x$ upto the term containing x^5 . (8)
- b. Find the value of a and b such that $\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$. (8)
- Q.3** a. Find the area of the segment cut off from the parabola $x^2 = 8y$ by the line $x - 2y + 8 = 0$. (8)
- b. Evaluate $\int_0^{\pi/2} \sin^4 x \cos^6 x dx$. (8)

Q.4 a. Express $\left[\frac{2 - \sqrt{3}i}{1 + i} \right]$ in the form $a + ib$ and find its modulus and amplitude. **(8)**

b. If n is positive integer, prove that $(\sqrt{3} + i)^n + (\sqrt{3} - i)^n = 2^{n+1} \cos\left(\frac{n\pi}{6}\right)$,
 $(i = \sqrt{-1})$ **(8)**

Q.5 a. Show that the points $-6i+3j+2k$, $3i-2j+4k$, $5i+7j+3k$ and $-13i+17j-k$ are coplanar. **(8)**

b. A particle acted on by, constant forces $4i+j-3k$ and $3i+j-k$ is displaced from the point $i+2j+3k$ to the point $5i+4j+k$. Find the total work done by the forces. **(8)**

Q.6 a. Solve the differential equation $\frac{d^3 y}{dx^3} + 2\frac{d^2 y}{dx^2} + \frac{dy}{dx} = e^{-x} + \sin 2x$. **(8)**

b. Solve the differential equation $\frac{d^2 y}{dx^2} - 3\frac{dy}{dx} + 2y = xe^{3x} + \cos 2x$. **(8)**

Q.7 a. Find the fourier series expansion of $f(x) = 2x - x^2$ in the interval $0 \leq x \leq 2$. **(8)**

b. Obtain the fourier expansion of $f(x) = x \sin x$ as a cosine series in $(0, \pi)$. **(8)**

Q.8 a. Find the Laplace transform of $[t^3 e^{-2t} \sin 4t]$. **(8)**

b. Find the Laplace transform of $\left[\frac{\cos at - \cos bt}{t} \right]$. **(8)**

Q.9 a. Apply Convolution theorem to evaluate $L^{-1}\left[\frac{1}{s^2(s^2 + 9)} \right]$. **(8)**

b. Using Laplace transform, solve the differential equation $Y'' + 4Y' + 4Y = 0$, given that $Y(0) = 0$ and $Y'(0) = 1$. **(8)**