

AMIETE – ET/CS/IT (Current & New Scheme)

Time: 3 Hours

December 2016

Max. Marks: 100

PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q1. Choose the correct or the best alternative in the following. (2×10)

a. The discrete LTI system is represented by impulse response $h(n)=(1/3)^n u(n)$, then the system is

- (A) Noncausal and stable (B) Noncausal and unstable
(C) Causal and stable (D) Causal and unstable

b. The evolution of the following integral is

$$x(t) = \int_{-\infty}^{+\infty} (t^3 + \cos \pi t) \cdot \delta(t-1) \cdot dt$$

- (A) 0 (B) π
(C) ∞ (D) t

c. The impulse response of the system is given by $h(n) = (3)^n u[n]$, then the output of the system for the input $x(n)=u(n)$ is

- (A) $\left[(3)^{n+1} + 1 \right] u[n]$ (B) $\left[(3)^{n+1} - 1 \right] u[n]$
(C) $\left[(3)^n + 1 \right] u[n]$ (D) $\left[(3)^{n-1} - 1 \right] u[n]$

d. The signal $x[n] = \cos\left(\frac{n\pi}{12}\right) + \sin\left(\frac{n\pi}{9}\right)$ is periodic with a period equal to

- (A) 12 (B) 18
(C) 72 (D) 36

e. The frequency response of the system $h(n)=[\delta(n+1)+ \delta(n-1)]$ is

- (A) $\sin w$ (B) $2\cos w$
(C) $\cos 2w$ (D) $\sin 2w$

f. The Fourier Transform of the function $x(t) = \text{sgn}(t)$ is

- (A) $\frac{2}{j\omega}$ (B) $\frac{4}{j\omega}$
(C) $\frac{1}{j\omega}$ (D) $\frac{1}{j\omega} + 1$

g. The convolution of signal $x(n) = 2^n u(n)$ with $h(n) = 3^n u(n)$ is

- (A) $[3^{n+1} - 2n] u(n)$ (B) $[3^{n+1} - 2^{n+1}] u(n)$
 (C) $[3^{n+1} - 2^{n+1}] u(n)$ (D) $[3^{n+1} - 2^{n+1}] u(n)$

h. The Laplace Transform of $X(t) = e^{-3t} \sin(2t)u(t)$ is

- (A) $\frac{s}{(s+2)^2+3}$ (B) $\frac{s}{(s+3)^2+4}$
 (C) $\frac{s}{(s+2)+3}$ (D) $\frac{s}{(s+3)+4}$

i. The Z-transform of $x(n) = (1/2)^n u(-n)$ is

- (A) $\frac{1}{1+2z}$ (B) $\frac{z}{1+2z}$
 (C) $\frac{1}{1-2z}$ (D) $\frac{1}{2+z}$

j. The density function of a random variable X is expressed as

$$f_x(x) = \begin{cases} ae^{-ax} & x > 0; \quad a = \text{constant} \\ 0 & \text{otherwise} \end{cases}$$

Then, its expected values $E[x]$ is

- (A) $1/a$ (B) e^{-a}
 (C) a (D) $a e^{-a}$

Answer any FIVE Questions out of EIGHT Questions.

Each question carries 16 marks.

Q.2 a. Explain the following signals with suitable examples (4)

- (i) Periodic and non-periodic signals
 (ii) Deterministic and random signals

b. For the signal $x(t)$ shown in figure-1, find (6)

- (i) $x(t-1)u(t)$
 (ii) $x(2t-1)$
 (iii) $x(-2t+1)$

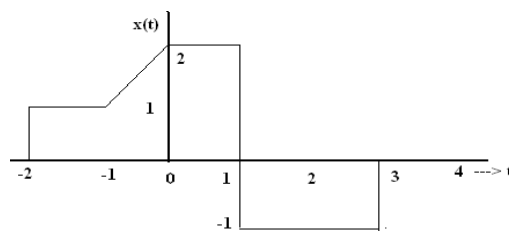


Figure-1

c. The impulse response of the system is given by (6)

$$h(n) = \left(\frac{1}{2}\right)^n u(n+1)$$

Determine whether the corresponding system is memoryless causal and stable.

Q.3 a. Determine the Fourier's Series representation for the following signals (10)

(i) $x(t) = 1 + 2 \cos(\omega_o t) + \sin(\omega_o t) + \cos\left(2\omega_o t + \frac{\pi}{4}\right)$

(ii) $x(n) = 1 + \sin\left[\frac{\pi}{12}n + \frac{\pi}{3}\right]$

b. Find the Fourier Series representation of the signal $x(n)$ shown in figure-2 (6)

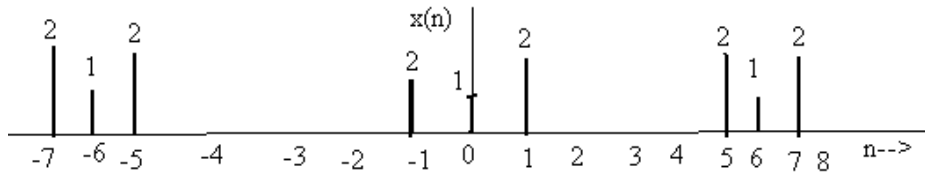


Figure-2

Q.4 a. State and prove the following properties of continuous signal Fourier Transform. (8)

- (i) Time shifting property
- (ii) Convolution property

b. Find the Fourier Transform of the signal $x(t) = (1-t)e^{-2t} u(t)$ (4)

c. Find the Inverse Fourier Transform of (4)

$$X(j\omega) = \frac{j\omega}{(j\omega)^2 + 3(j\omega) + 2}$$

Q.5 a. Find the Fourier transform of periodic signal $x[n] = \cos \omega_o n$, with $\omega_o = 2\pi/5$ and plot it. (6)

b. A causal LTI system is described by the difference equation (6)

$$3y(n) - 4y(n-1) + y(n-2) = 3x(n)$$

- (i) The system Transfer function.
- (ii) The unit sample response of system.

c. State and prove time shifting property of Discrete-time Fourier Transform. (4)

Q.6 a. The impulse response of the system is given by (6)

$$h(t) = e^{(1+t)} u(-t+2)$$

find its frequency response

b. Why sampling is required? Explain sampling theorem for a Low pass signal and also discuss how information can be reconstructed from the sample values? (6)

c. Determine the Nyquist rate of sampling for the following signals (4)

(i) $x(t) = 1 + \sin(200\pi t) - \sin(300\pi t)$

(ii) $x(t) = \cos^2(600\pi t)$

- Q.7** a. Find the Laplace transform of the following signals. (8)
- (i) $X(t) = e^{-2t}u(t) + e^{-t} \cos(3t)u(t)$
- (ii) $x(t) = e^{-b|t|}$
- b. Find the Inverse Laplace transform of the following $X(s)$ (4)
- $$X(S) = \frac{3}{(S^2 + 10S + 34)}$$
- c. State the properties of ROC in Laplace transform. (4)
- Q.8** a. Find the Z-transform of the following sequence and find the ROC (6)
- (i) $x[n] = 3\left(\frac{1}{2}\right)^n u[n] - 5(3)^n u[-n - 1]$
- (ii) $x[n] = 2n^2 u[n]$
- b. State and prove the Scaling property of Z- transform (4)
- c. The system equation is given by (6)
- $$y(n) - (7/2)y(n-1) + (3/2)y(n-2) = 3x(n) - 4x(n-1)$$
- Determine
- (i) Transfer function $H(Z)$
- (ii) Impulse response $h(n)$, assuming System is causal.
- Q.9** a. For a stationary Ergodic process $X(t)$ if autocorrelation function $R_x(\tau)$ is given (4)
- $$\text{by } R_x(\tau) = \frac{\tau^2}{2 + 4\tau^2}$$
- Then find the mean and variance of $X(t)$ (4)
- b. Write a note on Gaussian noise (4)
- c. Define the following terms with reference to probability theory (8)
- (i) Wide sense stationary process
- (ii) Power spectral density
- (iii) Conditional probability
- (iv) Covariance function